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-	91	378/5.ccls.	USPAT; US-PGPUB; EPO; JPO; IBM_TDB	2004/05/04 10:25
-	229	378/156.ccls.	USPAT; US-PGPUB; EPO; JPO; IBM_TDB	2004/04/27 16:36
-	1	avinash-gopal.in.	USPAT; US-PGPUB; EPO; JPO; IBM_TDB	2004/04/27 16:39
-	55	avinash-gopal-b.in.	USPAT; US-PGPUB; EPO; JPO; IBM_TDB	2004/04/27 16:38
-	5	SABOL-JOHN-MICHAEL.in.	USPAT; US-PGPUB; EPO; JPO; IBM_TDB	2004/04/27 16:38
-	11	NICOLAS-FRANCOIS-SERGE.in.	USPAT; US-PGPUB; EPO; JPO; IBM_TDB	2004/04/27 16:38
-	63	avinash-gopal.in. avinash-gopal-b.in. SABOL-JOHN-MICHAEL.in. NICOLAS-FRANCOIS-SERGE.in.	USPAT; US-PGPUB; EPO; JPO; IBM_TDB	2004/04/27 16:39
-	42	(avinash-gopal.in. avinash-gopal-b.in. SABOL-JOHN-MICHAEL.in. NICOLAS-FRANCOIS-SERGE.in.) and (xray$2 x$ray$2)	USPAT; US-PGPUB; EPO; JPO; IBM_TDB	2004/04/27 16:39
-	610	378/62.ccls.	USPAT; US-PGPUB; EPO; JPO; IBM_TDB	2004/04/27 16:59
-	69	378/98.11.ccls.	USPAT; US-PGPUB; EPO; JPO; IBM_TDB	2004/05/12 17:26
-	84	378/98.9.ccls.	USPAT; US-PGPUB; EPO; JPO; IBM_TDB	2004/05/11 15:40

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-	3972	(xray2 xray$3) same (energ$4 power heat) same (bon$4 tissu$3)	USPAT; US-PGPUB; EPO; JPO; IBM_TDB	2004/04/28 14:36
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-	1	6580779.pn.	USPAT;	2004/05/03 14:19
-	0	6580779.URPN.	USPAT	2004/05/03 14:20
-	3	("6052433" | "6343111" | "6501819" | "2002/0186872").PN.	USPAT	2004/05/03 14:20
-	4	6343111.URPN.	USPAT	2004/05/03 14:32
-	234	378/98.12.ccls.	USPAT;	2004/05/03 15:25
-	8960	(character$6 gradient$4 localizat$6) near4 (mask$3)	USPAT; US-PGPUB; EPO; JPO; IBM_TDB	2004/05/03 15:29
-	962	((character$6 gradient$4 localizat$6) near4 (mask$3)) same (energ$4 power$3 heat$3)	USPAT; US-PGPUB; EPO; JPO; IBM_TDB	2004/05/03 15:29
-	16	(((character$6 gradient$4 localizat$6) near4 (mask$3)) same (energ$4 power$3 heat$3)) same (bon$2 tissue$2 anatom$3)	USPAT; US-PGPUB; EPO; JPO; IBM_TDB	2004/05/03 15:29
-	9	(((character$6 gradient$4 localizat$6) near4 (mask$3)) same (energ$4 power$3 heat$3)) same (bone$2 tissue$2 anatom$3)	USPAT; US-PGPUB; EPO; JPO; IBM_TDB	2004/05/03 15:29

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22	4355331.URPN.	USPAT	2004/05/04 10:58

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-	1648	energy near3 subtract$4	USPAT; US-PGPUB; EPO; JPO; IBM_TDB	2004/05/10 10:22
-	218	(energy near3 subtract$4) and (noise near3 reduc$5)	USPAT; US-PGPUB; EPO; JPO; IBM_TDB	2004/05/10 16:57
-	19	((energy near3 subtract$4) and (noise near3 reduc$5)) and (gradient)	USPAT; US-PGPUB; EPO; JPO; IBM_TDB	2004/05/10 10:25
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-	1	"20020186872" and (character$5 near3 mask$3)	USPAT; US-PGPUB; EPO; JPO; IBM_TDB	2004/05/10 17:17
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-	888	(bone and tissue) and pixel$2 and (white light) and (black dark)	USPAT; US-PGPUB; EPO; JPO; IBM_TDB	2004/05/10 17:58
-	457	((bone and tissue) and pixel$2 and (white light) and (black dark)) and energy	USPAT; US-PGPUB; EPO; JPO; IBM_TDB	2004/05/10 17:20
-	222	(((bone and tissue) and pixel$2 and (white light) and (black dark)) and energy) and subtract$4	USPAT; US-PGPUB; EPO; JPO; IBM_TDB	2004/05/10 17:21
-	68	((((bone and tissue) and pixel$2 and (white light) and (black dark)) and energy) and subtract$4) and (reduc$4 near3 noise)	USPAT; US-PGPUB; EPO; JPO; IBM_TDB	2004/05/10 17:21
-	20	((bone and tissue) and pixel$2 and (white light) and (black dark)) and (energy near3 subtract$4)	USPAT; US-PGPUB; EPO; JPO; IBM_TDB	2004/05/10 17:59

-	13	((bone and tissue) and pixel$2 and (white light) and (black dark)) and (energy near3 subtract$4)) and (reduc$4 near3 noise)	USPAT; US-PGPUB; EPO; JPO; IBM_TDB	2004/05/10 18:00
-	35	(bone and tissue) and (pixel$2 near3 (white light) near3 (black dark))	USPAT; US-PGPUB; EPO; JPO; IBM_TDB	2004/05/10 17:59
-	1	((bone and tissue) and (pixel$2 near3 (white light) near3 (black dark))) and (energy near5 subtract$4)	USPAT; US-PGPUB; EPO; JPO; IBM_TDB	2004/05/10 18:00
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-	7	((bone and tissue) and (pixel$2 near3 (white light) near3 (black dark))) and (reduc$4 near5 noise)	USPAT; US-PGPUB; EPO; JPO; IBM_TDB	2004/05/10 18:00
-	7	((bone and tissue) and (pixel$2 near3 (white light) near3 (black dark))) and (reduc$4 near5 nois$4)	USPAT; US-PGPUB; EPO; JPO; IBM_TDB	2004/05/10 18:00
-	3	(((bone and tissue) and (pixel$2 near3 (white light) near3 (black dark))) and (reduc$4 near5 nois$4)) and (energy)	USPAT; US-PGPUB; EPO; JPO; IBM_TDB	2004/05/12 17:24
-	9	(US-6661873-$ or US-6701025-$ or US-6501819-$ or US-6597759-$ or US-4792900-$ or US-6205348-$ or US-4355331-$ or US-5301107-$).did. or (US-20030095630-$).did.	USPAT; US-PGPUB	2004/05/11 15:31
-	7	(US-6661873-$ or US-6701025-$ or US-6501819-$ or US-6597759-$ or US-4792900-$ or US-6205348-$ or US-4355331-$ or US-5301107-$).did. or (US-20030095630-$).did.) and (list$3 table group)	USPAT; US-PGPUB; EPO; JPO; IBM_TDB	2004/05/12 14:27
-	23435	(determin$4 measur43 obtain$4 get$4 generat$4) near4 (gradient$3)	USPAT; US-PGPUB; EPO; JPO; IBM_TDB	2004/05/11 15:36
-	236	((determin$4 measur43 obtain$4 get$4 generat$4) near4 (gradient$3)) same (energ$4) same (imag$4)	USPAT; US-PGPUB; EPO; JPO; IBM_TDB	2004/05/11 15:36
-	5	(((determin$4 measur43 obtain$4 get$4 generat$4) near4 (gradient$3)) same (energ$4) same (imag$4)) same (nois$4 near4 reduc$5)	USPAT; US-PGPUB; EPO; JPO; IBM_TDB	2004/05/11 15:37
-	0	378/98.11.ccls. and (((determin$4 measur43 obtain$4 get$4 generat$4) near4 (gradient$3)) same (energ$4) same (imag$4))	USPAT; US-PGPUB; EPO; JPO; IBM_TDB	2004/05/11 15:40

		Search Query	Databases	Date/Time
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-	1	378/98.9.ccls. and (((determin$4 measur43 obtain$4 get$4 generat$4) near4 (gradient$3)) same (energ$4) same (imag$4))	USPAT; US-PGPUB; EPO; JPO; IBM_TDB	2004/05/11 15:41
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-	32	4499493.URPN.	USPAT	2004/05/11 15:43
-	1	4499493.pn. and gradient$3	USPAT; US-PGPUB; EPO; JPO; IBM_TDB	2004/05/11 16:09
-	1	5402338.pn.	USPAT; US-PGPUB; EPO; JPO; IBM_TDB	2004/05/12 13:02
-	7	5402338.URPN.	USPAT	2004/05/12 11:39
-	0	5402338.pn. and (gradient$3)	USPAT; US-PGPUB; EPO; JPO; IBM_TDB	2004/05/12 13:02
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-	11	(US-6501819-$ or US-6701025-$ or US-6661873-$ or US-6597759-$ or US-6205348-$ or US-5301107-$ or US-4792900-$ or US-4355331-$ or US-4499493-$ or US-5402338-$).did. or (US-20030095630-$).did.	USPAT; US-PGPUB	2004/05/12 14:27
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-	512	((bone and tissue)and (reduc$4 near5 nois$4) and (energ$3)) and (lut or (look near up near table) or list)	USPAT; US-PGPUB; EPO; JPO; IBM_TDB	2004/05/12 17:25
-	5	378/98.9.ccls. and (((bone and tissue)and (reduc$4 near5 nois$4) and (energ$3)) and (lut or (look near up near table) or list))	USPAT; US-PGPUB; EPO; JPO; IBM_TDB	2004/05/12 18:09
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-	17477	(gradient) and ((low or high) near4 (energ$4))	USPAT; US-PGPUB; EPO; JPO; IBM_TDB	2004/05/12 18:09
-	660	(gradient) with ((low or high) near4 (energ$4))	USPAT; US-PGPUB; EPO; JPO; IBM_TDB	2004/05/12 18:09
-	15	((gradient) with ((low or high) near4 (energ$4))) same ratio	USPAT; US-PGPUB; EPO; JPO; IBM_TDB	2004/05/12 18:10
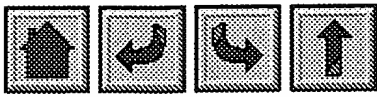
Sobel Edge Detector

Common Names: Sobel, also related is Prewitt Gradient Edge Detector

Brief Description

The Sobel operator performs a 2-D spatial gradient measurement on an image and so emphasizes regions of high spatial gradient that correspond to edges. Typically it is used to find the approximate absolute gradient magnitude at each point in an input greyscale image.

How It Works

In theory at least, the operator consists of a pair of 3×3 convolution masks as shown in Figure 1. One mask is simply the other rotated by 90°. This is very similar to the Roberts Cross operator.

-1	0	+1
-2	0	+2
-1	0	+1

Gx

+1	+2	+1
0	0	0
-1	-2	-1

Gy

Figure 1 Sobel convolution masks

These masks are designed to respond maximally to edges running vertically and horizontally relative to the pixel grid, one mask for each of the two perpendicular orientations. The masks can be applied separately to the input image, to produce separate measurements of the gradient component in each orientation (call these *Gx* and *Gy*). These can then be combined together to find the absolute magnitude of the gradient at each point and the orientation of that gradient. The gradient magnitude is given by:

$$|G| = \sqrt{Gx^2 + Gy^2}$$

Although typically, an approximate magnitude is computed using:

$$|G| = |Gx| + |Gy|$$

which is much faster to compute.

The angle of orientation of the edge (relative to the pixel grid) giving rise to the spatial gradient is given by:

$$\theta = \arctan(Gy/Gx) - 3\pi/4$$

In this case, orientation 0 is taken to mean that the direction of maximum contrast from black to white runs from left to right on the image, and other angles are measured anti-clockwise from this.

Often, this absolute magnitude is the only output the user sees --- the two components of the gradient are conveniently computed and added in a single pass over the input image using the pseudo-convolution operator shown in Figure 2.

P_1	P_2	P_3
P_4	P_5	P_6
P_7	P_8	P_9

Figure 2 Pseudo-convolution masks used to quickly compute approximate gradient magnitude

Using this mask the approximate magnitude is given by:

$$|G| = |(P_1 + 2 \times P_2 + P_3) - (P_7 + 2 \times P_8 + P_9)| + |(P_3 + 2 \times P_6 + P_9) - (P_1 + 2 \times P_4 + P_7)|$$

Guidelines for Use

The Sobel operator is slower to compute than the Roberts Cross operator, but its larger convolution mask smooths the input image to a greater extent and so makes the operator less sensitive to noise. The operator also generally produces considerably higher output values for similar edges compared with the Roberts Cross.

As with the Roberts Cross operator, output values from the operator can easily overflow the maximum allowed pixel value for image types that only support smallish integer pixel values (*e.g.* 8-bit integer images). When this happens the standard practice is to simply set overflowing output pixels to the maximum allowed value. The problem can be avoided by using an image type that supports pixel values with a larger range.

Natural edges in images often lead to lines in the output image that are several pixels wide due to the smoothing effect of the Sobel operator. Some thinning may be desirable to counter this. Failing that, some sort of hysteresis ridge tracking could be used as in the Canny operator.

 shows the results of applying the Sobel operator to . Compare this with the equivalent Roberts cross output . Note that the spurious noise that afflicted the Roberts cross output image is still present in this image, but its intensity relative to the genuine lines has been reduced, and so there is a good chance that we can get rid of this entirely by thresholding. Also notice that the lines corresponding to edges have become thicker compared with the Roberts cross output due to the increased smoothing of the Sobel operator.
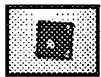
 shows a simpler scene containing just a single flat dark object against a lighter background. Applying the Sobel operator produces . Note that the lighting has been carefully set up to ensure that the edges of the object are nice and sharp and free of shadows.

The Sobel edge detector can also be applied to *range images* like . The corresponding edge image is . All edges in the image have been detected and can be nicely separated from the background using a threshold of *150*, as can be seen in .

Although the Sobel operator is not as sensitive to noise as the Roberts Cross operator, it still amplifies high frequencies. is the result of adding Gaussian noise with a standard deviation of *15* to the original image. Applying the Sobel operator yields and thresholding the result at a value of *150* produces . We can see that the noise has increased during the edge detection and it is not possible anymore to find a threshold which removes all noise pixels and at the same time retains the edges of the objects.

The object in the previous example contains sharp edges and its surface is rather smooth. Therefore, we could (in the noise free case) easily detect the boundary of the object without getting any erroneous pixels. A more difficult task is to detect the boundary of , because it contains many fine depth variations (*i.e.* resulting in intensity changes in the image) on its surface. Applying the Sobel operator straightforwardly yields . We can see that the intensity of many pixels on the surface is as high as along the actual edges. One reason is that the output of many edge pixels is greater than the maximum pixel value and therefore they are `cut off` at *255*. To avoid this overflow we scale the range image by a factor *0.25* prior to the edge detection and than normalize the output, as can be seen in . Although the result improved significantly, we still cannot find a threshold so that a closed line along the

boundary remains and all the noise disappears. Compare this image with the results obtained with the Canny edge detector.

Common Variants

A related operator is the Prewitt gradient edge detector (not to be confused with the Prewitt *compass edge detector*). This works in a very similar way to the Sobel operator but uses slightly different masks, as shown in Figure 3. This mask produces similar results to the Sobel, but is not as isotropic in its response.

-1	0	+1
-1	0	+1
-1	0	+1

Gx

+1	+1	+1
0	0	0
-1	-1	-1

Gy

Figure 3 Masks for the Prewitt gradient edge detector.

Exercises

1. Experiment with thresholding the example images to see if noise can be eliminated while still retaining the important edges.

2. How does the Sobel operator compare with the Roberts cross operator in terms of noise rejection, edge detection and speed?

3. How well are the edges located using the Sobel operator? Why is this?

4. Apply the Sobel operator to ▢ and see if you can use thresholding to detect the edges of the object without obtaining noise. Compare the results with the one obtained with the Roberts cross operator.

5. Under what conditions would you want to use the Sobel rather than the Roberts cross operator? And when would you not want to use it?

References

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E. Davies *Machine Vision: Theory, Algorithms and Practicalities* Academic Press, 1990, Chap 5.

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Local Information

General advice about the local HIPR installation is available <u>here</u>

Hypermedia Image Processing Reference